

***CP* VIOLATION IN PSEUDO-DIRAC FERMION OSCILLATIONS**

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Sneak peek

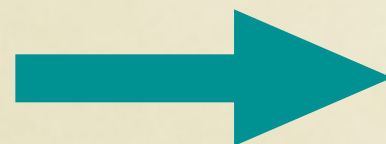
- We need to have more CP violation for baryogenesis
- $U(1)_R$ symmetric SUSY brings new CP violation without EDM constraints
 - This model also has (pseudo-)Dirac fermions
 - Pseudo-Dirac fermions have oscillations between Dirac partners
 - There can be CP violation in these oscillations
 - This CP violation can give rise to a same sign dilepton asymmetry

CP Violation in the Standard Model

Only source: Quark mixing matrix (CKM matrix)

$$-\frac{g}{\sqrt{2}} (\bar{u} \ \bar{c} \ \bar{t}) \gamma^\mu W_\mu^+ \underbrace{\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}}_{V_{\text{CKM}}} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

V_{CKM} : 3 mixing angles + 1 irreducible phase

 *CP* violation in the electroweak sector

We need (more) *CP* violation

Our Universe has a lot more matter than antimatter!

How?

baryogenesis: Produce 10^8+1 quarks for every 10^8 antiquarks

- Baryon number violation
- *CP* violation
- Out-of-equilibrium conditions



CKM phase gives an asymmetry of $\sim 10^{-20}$

suppressed by small mixing angles and Yukawa couplings



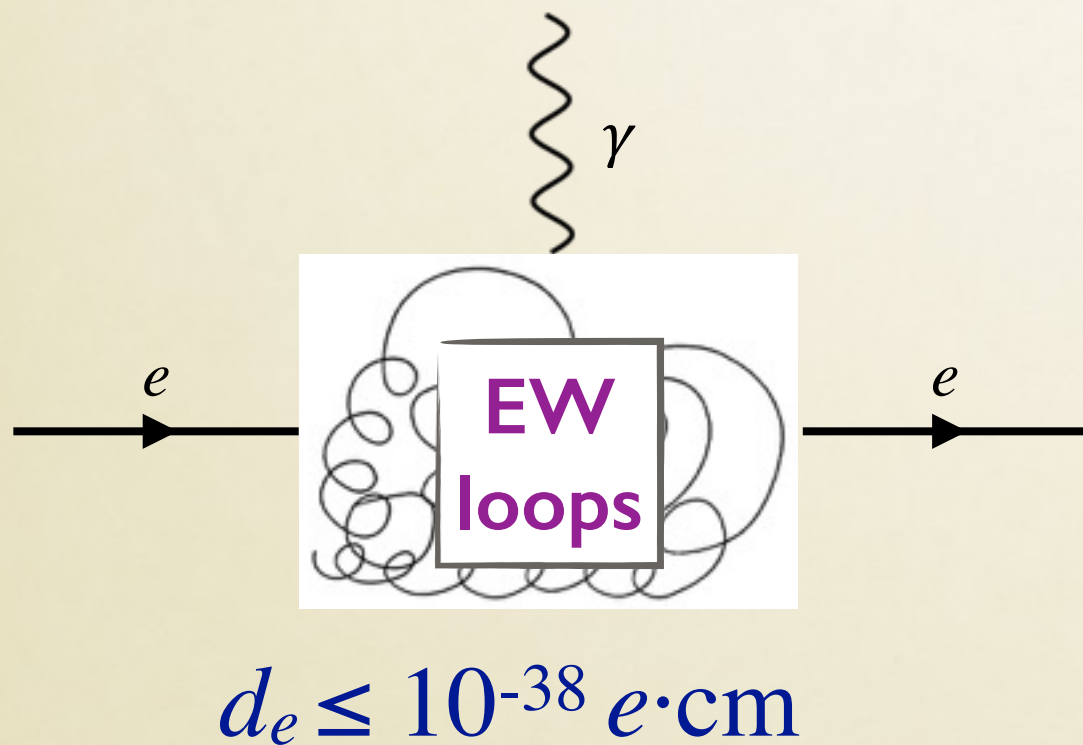
We need more *CP* violation!

EDM Constraints on CP Violation

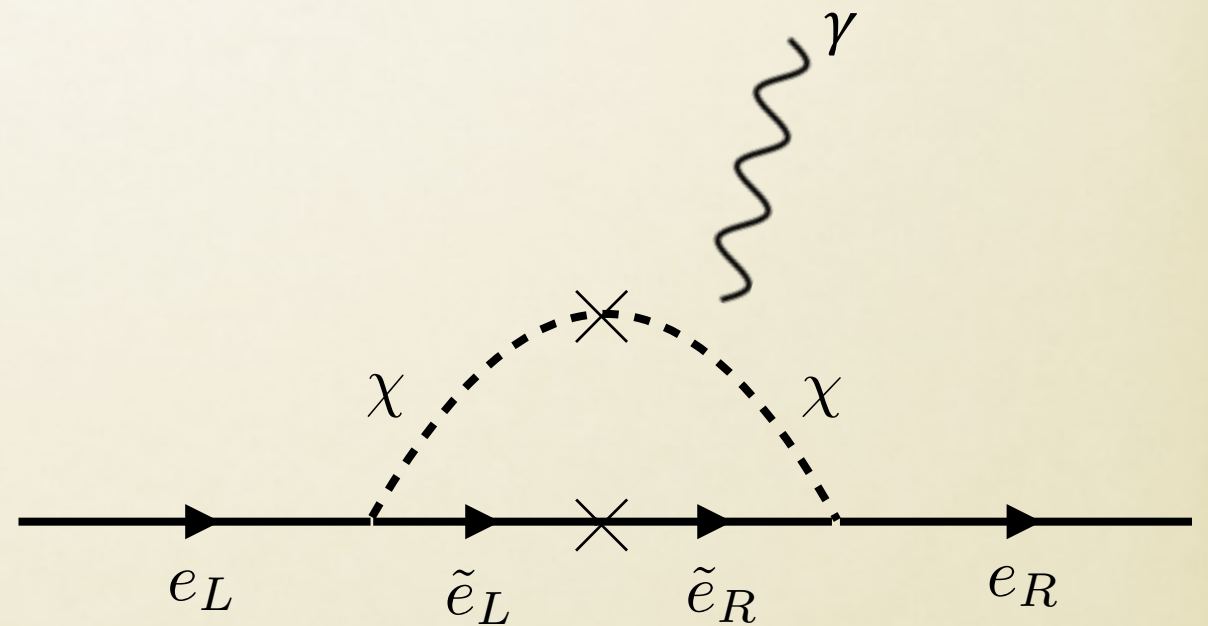
Electron electric dipole moment: $d_e \leq 0.87 \times 10^{-28} e \cdot \text{cm}$

ACME, *Science* 343 (2014)

What we have in the SM:



What SUSY has:



SUSY CP problem

Solution: $U(1)_R$ symmetric SUSY

Part of the field content:

Field	$SU(3)$	$SU(2)$	$U(1)$	$U(1)_R$
q_i	3	2	1/6	0
\bar{u}_i	$\bar{3}$	1	$-2/3$	0
\bar{d}_i	$\bar{3}$	1	1/3	0
ℓ_i	1	2	$-1/2$	0
\bar{e}_i	1	1	1	0
$\phi_{\bar{d}_i}$	$\bar{3}$	1	1/3	+1
λ	8	1	0	+1

SM fermions are not charged under $U(1)_R$

Sfermions and gauginos have +1 $U(1)_R$ charge

Hall, Randall, *Nuc.Phys.B*-352.2 1991

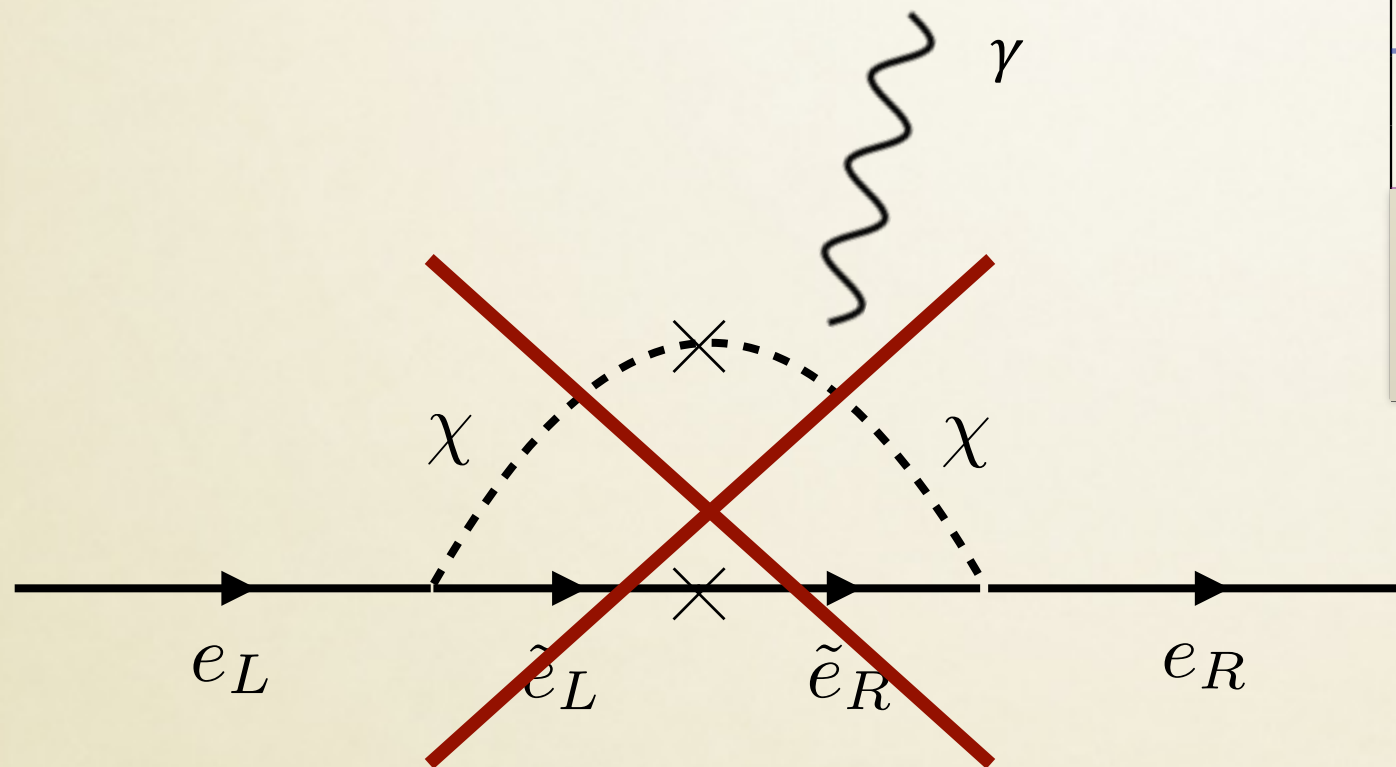
Kribs, Poppitz, Weiner, *PRD* 78 2007

Electron EDM in $U(1)_R$ symmetric SUSY

Due to the $U(1)_R$ symmetry

- No Majorana masses for gauginos
- No left-right sfermion mixing

Field	$SU(3)$	$SU(2)$	$U(1)$	$U(1)_R$
q_i	3	2	1/6	0
\bar{u}_i	$\bar{3}$	1	-2/3	0
\bar{d}_i	$\bar{3}$	1	1/3	0
ℓ_i	1	2	-1/2	0
\bar{e}_i	1	1	1	0
$\phi_{\bar{d}_i}$	$\bar{3}$	1	1/3	+1
λ	8	1	0	+1



We can have large CP violating parameters without constraint

Hall, Randall, *Nuc.Phys.B*-352.2 1991

Kribs, Poppitz, Weiner, *PRD* 78 2007

Need more fields

Make Dirac gauginos:

Field	$SU(3)$	$SU(2)$	$U(1)$	$U(1)_R$
q_i	3	2	1/6	0
\bar{u}_i	$\bar{3}$	1	-2/3	0
\bar{d}_i	$\bar{3}$	1	1/3	0
ℓ_i	1	2	-1/2	0
\bar{e}_i	1	1	1	0
$\phi_{\bar{d}_i}$	$\bar{3}$	1	1/3	+1
λ	8	1	0	+1
\mathcal{O}	8	1	0	-1

SM fermions are not charged under $U(1)_R$

Sfermions and gauginos have +1 $U(1)_R$ charge

← Dirac partner of gluino a.k.a. octino

Hall, Randall, *Nuc.Phys.B*-352.2 1991

Kribs, Poppitz, Weiner, *PRD* 78 2007

Dirac fermions in $U(1)_R$ symmetric SUSY

- Dirac masses for gauginos \rightarrow new chiral adjoints

e.g. $\lambda \equiv (8, 1, 0)_{+1}$ gluino

$\mathcal{O} \equiv (8, 1, 0)_{-1}$ Dirac partner of gluino \equiv octino

- λ and \mathcal{O} are two (Weyl) components of a Dirac gluino

$$\psi = \begin{pmatrix} \lambda \\ i\sigma_2 \mathcal{O}^* \end{pmatrix}$$

with conserved $U(1)_R$ charge and a Dirac mass

$$-\mathcal{L}_{\text{mass}} = m_D \lambda \mathcal{O} + m_D^* \lambda^\dagger \mathcal{O}^\dagger$$

Pseudo-Dirac fermions

- $U(1)_R$ symmetry is always broken by supergravity!
- Approximate $U(1)_R \rightarrow$ Majorana masses for the gluino partners:

$$-\delta\mathcal{L}_{\text{mass}} = \frac{1}{2} (m_\lambda \lambda\lambda + m_{\mathcal{O}} \mathcal{O}\mathcal{O}) + \text{h.c.}$$

$$\psi = \begin{pmatrix} \lambda \\ i\sigma_2 \mathcal{O}^* \end{pmatrix} \rightarrow \textbf{Pseudo-Dirac fermion}$$

$$\mathcal{H}_{\text{mass}} = \begin{pmatrix} m_D & m_M \\ m_M^* & m_D \end{pmatrix} \quad m_M = \frac{1}{2}(m_\lambda^* + m_{\mathcal{O}})$$

with mass eigenvalues: $M_{1,2} = m_D \pm |m_M|$

corresponding eigenstates: $\frac{1}{\sqrt{2}} (|\psi\rangle \pm e^{-i\phi} |\bar{\psi}\rangle) \quad \phi = \arg(m_M)$

Pseudo-Dirac fermion oscillations

- Mass eigenstates \neq interaction eigenstates
 \Rightarrow oscillations

- A pseudo-Dirac fermion has 4 states:

$$(R^+, \uparrow), (R^+, \downarrow), (R^-, \uparrow), (R^-, \downarrow)$$

- Oscillations mix only 2×2 blocks:

work with 2-component
Weyl spinors

- (R^+, \uparrow) can oscillate into (R^-, \uparrow)
- (R^+, \downarrow) can oscillate into (R^-, \downarrow)

Dreiner, Haber, Martin, *arXiv:0812.1594*

- Examples: neutrinos, mesinos, neutralinos

Wolfenstein, *Nucl Phys B* 186 (1981), ...

Thomas, Sarid, *PRL* 85 (2000)

Grossman, Shakya, Tsai, *PRD* 88 (2013)

Interactions: toy model

Consider the $U(1)_R$ -violating interactions:

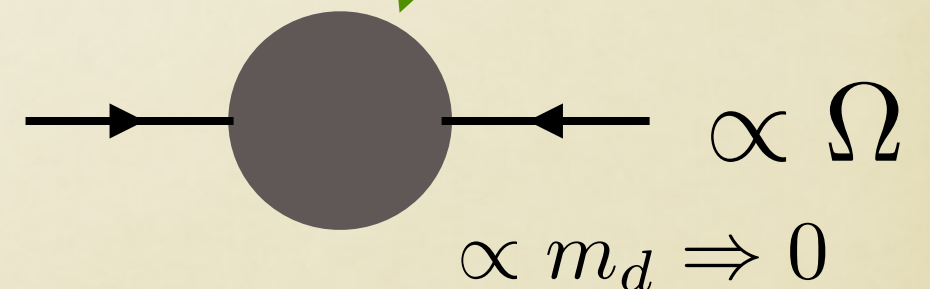
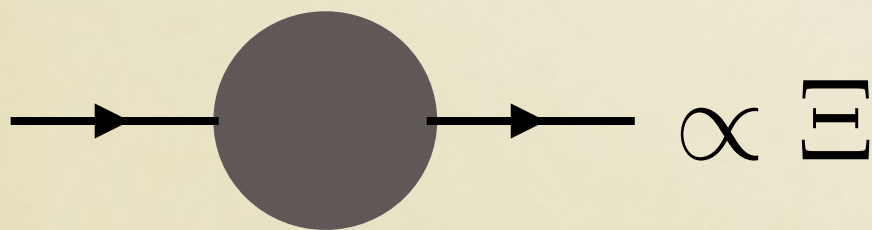
$$\mathcal{L}_{\text{int}} = -\phi^* (y_\lambda \lambda^a + y_{\mathcal{O}} \mathcal{O}^a) t^a \bar{d} + \text{h.c.}$$

ϕ = complex scalar (squark), d = fermion (quark), $t^a = SU(3)$ generator

➔ $M_{1,2}$ are modified

Solve: $\det \left[\textcolor{red}{s}1 - (1 - \Xi^T)^{-1} (m + \Omega) (1 - \Xi)^{-1} (\bar{m} + \bar{\Omega}) \right] = 0$

$$m = \begin{pmatrix} m_\lambda & m_D \\ m_D & m_{\mathcal{O}} \end{pmatrix}$$



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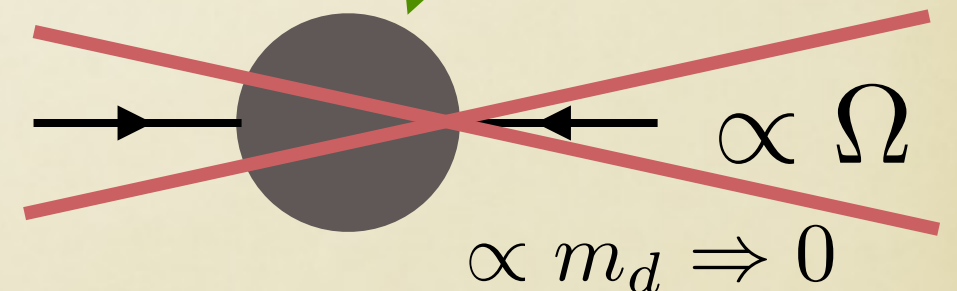
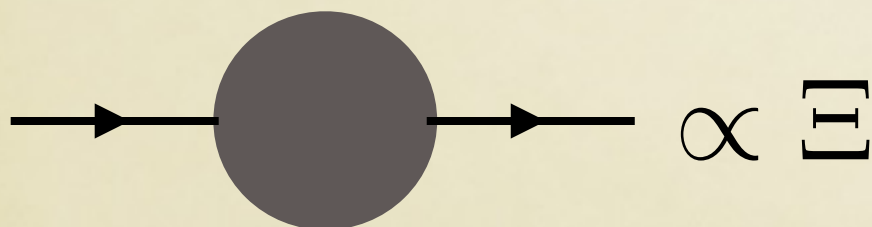
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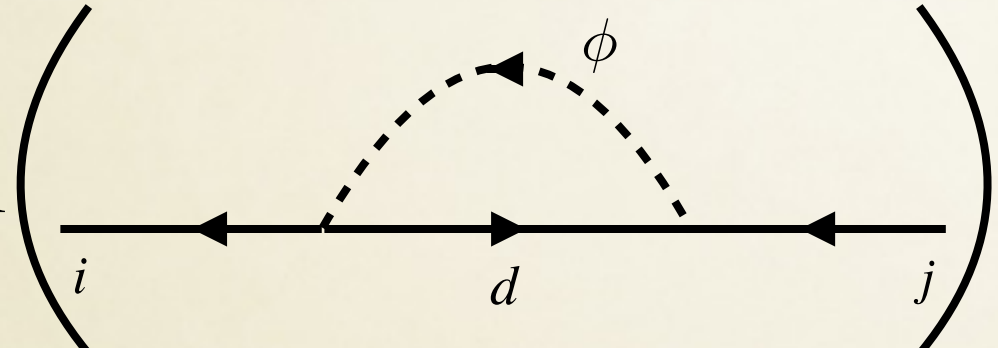
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Interaction Hamiltonian

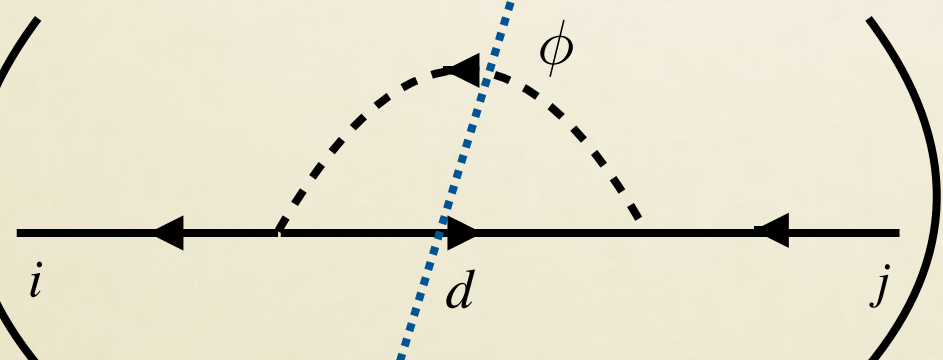
$\mathcal{H}_{\text{mass}} + \text{interactions} \Rightarrow \text{effective Hamiltonian}$

$$H = M + \frac{i}{2}\Gamma$$

● Real  → corrections to masses

$i, j = \lambda, \mathcal{O}$

$$M = \begin{pmatrix} M_D & M_M \\ M_M^* & M_D \end{pmatrix}$$

● Imaginary  → Width

$$\Gamma \simeq \frac{M_D}{64\pi} \left(1 - \frac{m_\phi^2}{M_D^2} \right)^2 \begin{pmatrix} |y_\lambda|^2 + |y_{\mathcal{O}}|^2 & 2y_\lambda y_{\mathcal{O}}^* \\ 2y_\lambda^* y_{\mathcal{O}} & |y_\lambda|^2 + |y_{\mathcal{O}}|^2 \end{pmatrix}$$

Back to *real* life

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2-component Weyl spinors

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Dirac partner of gluino

Extra superpartners

- λ is the lightest R -charged particle
- $\Phi_{D,\bar{D}} \rightarrow$ non-gauge couplings for $\Phi_{\mathcal{O}}$

Ipek, McKeen, Nelson, *arXiv*: 1407.8193

Why gluinos?

- Gluinos are produced strongly
- “[strong] interactions cause the state to decohere into a single mass eigenstate, thereby destroying the oscillation feature” **Grossman, Shakya, Tsai, *PRD* 88 (2013)**

$$\frac{\partial \rho}{\partial t} = -i [H, \rho] - \frac{\kappa}{2} [N, [N, \rho]] \quad \text{Tulin, Yu, Zurek, *JCAP* 1205 (2012)}$$

ρ = density matrix, κ = strength of interactions

$$\rho = \sum_{i,j=\psi,\bar{\psi}} |i\rangle\langle j|$$

modification due to:

$$\begin{aligned} \psi q &\rightarrow \psi q \\ \bar{\psi} q &\rightarrow \bar{\psi} q \end{aligned}$$

$$N = \text{diag}(1, -1) \quad \text{if} \quad \mathcal{L}_{int} \rightarrow -\mathcal{L}_{int} \quad \text{as} \quad \psi \rightarrow \bar{\psi}$$

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$$N = \text{diag}(1, +1) \quad \text{if} \quad \mathcal{L}_{int} \rightarrow +\mathcal{L}_{int} \quad \text{as} \quad \psi \rightarrow \bar{\psi}$$

ψ is an octet \longrightarrow real \longrightarrow strong interactions do NOT decohere ψ and $\bar{\psi}$

Dirac and Majorana masses

- Dirac gluino mass comes from:

$$\int d^2\theta \frac{c}{\Lambda_M} W'_\alpha W^\alpha \Phi_{\mathcal{O}} \quad \longrightarrow \quad m_D = \frac{cD}{\Lambda_M}$$

W'_α = spurion with a D -term, W^α = QCD superfield,

Λ_M = messenger scale, $\Phi_{\mathcal{O}}$ = superfield with \mathcal{O}

- Majorana mass for gluino (from anomaly mediation):

$$m_\lambda = \frac{\beta_s}{g_s} m_{3/2}$$

Randall, Sundrum, *Nucl.Phys.B* 352, 1991

Giudice, Luty, Murayama, Rattazzi, *JHEP* 9812, 1998

$m_{3/2}$ = gravitino mass, g_s = QCD coupling constant, β_s = beta function for g_s

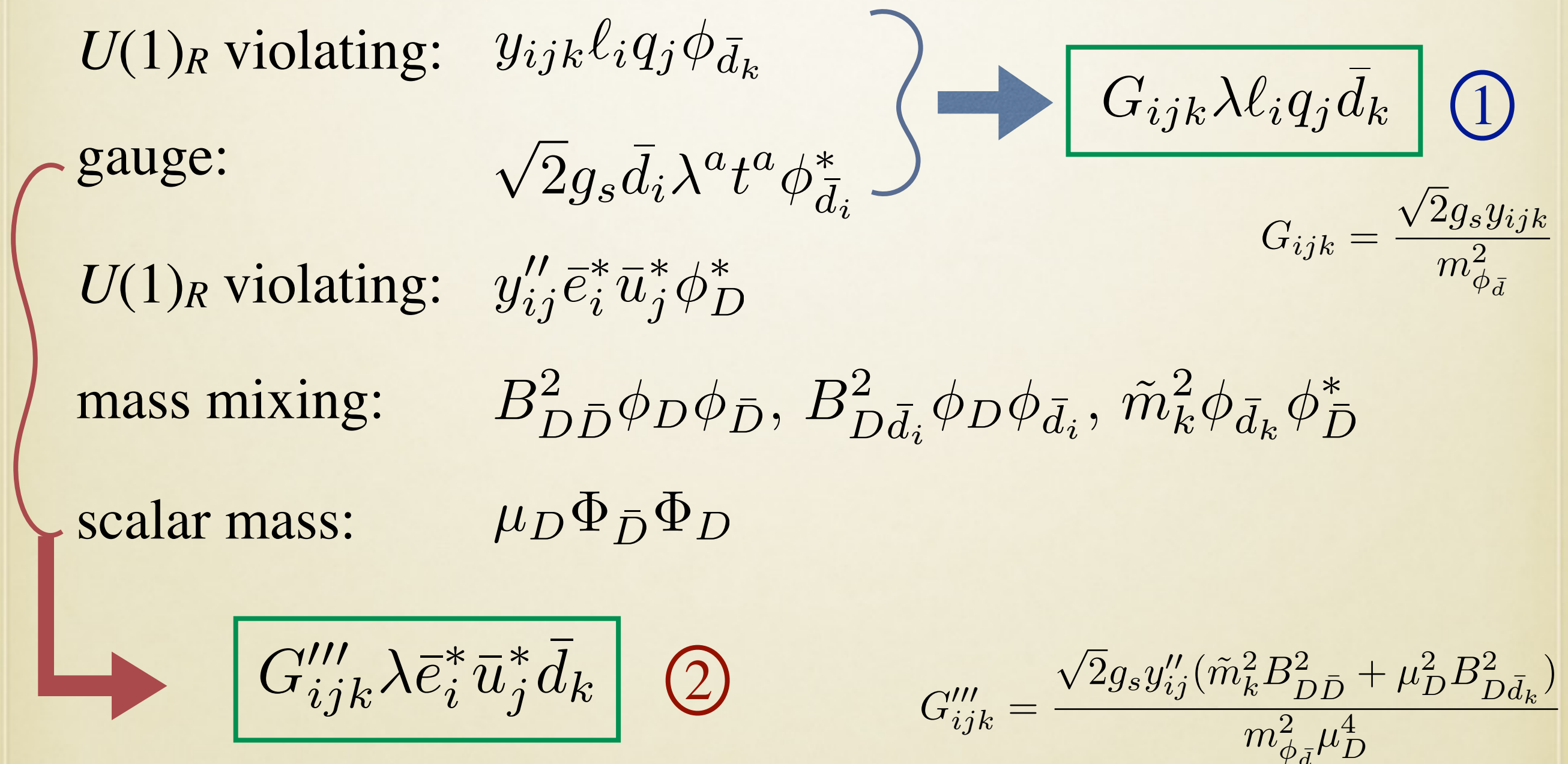
- Majorana mass for \mathcal{O} :

$$\int d^2\theta \, m_{\mathcal{O}} \Phi_{\mathcal{O}}^2 \quad \text{assume: } m_{\mathcal{O}} \ll m_D$$

4-fermion interactions: gluino

Warning: Messy!

$U(1)_R$ violating: $y_{ijk} \ell_i q_j \phi_{\bar{d}_k}$
 gauge: $\sqrt{2} g_s \bar{d}_i \lambda^a t^a \phi_{\bar{d}_i}^*$
 $U(1)_R$ violating: $y''_{ij} \bar{e}_i^* \bar{u}_j^* \phi_D^*$
 mass mixing: $B_{D\bar{D}}^2 \phi_D \phi_{\bar{D}}, B_{D\bar{d}_i}^2 \phi_D \phi_{\bar{d}_i}, \tilde{m}_k^2 \phi_{\bar{d}_k} \phi_{\bar{D}}^*$
 scalar mass: $\mu_D \Phi_{\bar{D}} \Phi_D$



$G_{ijk} = \frac{\sqrt{2} g_s y_{ijk}}{m_{\phi_{\bar{d}}}^2}$

$G'''_{ijk} = \frac{\sqrt{2} g_s y''_{ij} (\tilde{m}_k^2 B_{D\bar{D}}^2 + \mu_D^2 B_{D\bar{d}_k}^2)}{m_{\phi_{\bar{d}}}^2 \mu_D^4}$

4-fermion interactions: octino

More of the same:

$$\begin{array}{ll}
 U(1)_R \text{ violating:} & y''_{ij} \bar{e}_i^* \bar{u}_j^* \phi_D^* \\
 U(1)_R \text{ conserving:} & g'_i \bar{d}_i \mathcal{O}^a t^a \phi_D \\
 U(1)_R \text{ violating:} & y'_{ij} \ell_i q_j \phi_{\bar{D}} \\
 \text{mass mixing:} & B_{D\bar{D}}^2 \phi_D \phi_{\bar{D}}
 \end{array}
 \begin{array}{l}
 \left. \begin{array}{l} \text{red bracket} \\ \text{blue bracket} \end{array} \right\} \begin{array}{l} \rightarrow \\ \rightarrow \end{array}
 \end{array}
 \begin{array}{l}
 \boxed{G''_{ijk} \mathcal{O} \bar{e}_i^* \bar{u}_j^* \bar{d}_k} \quad \textcircled{3} \\
 \boxed{G'_{ijk} \mathcal{O} \ell_i q_j \bar{d}_k} \quad \textcircled{4}
 \end{array}$$

$$G''_{ijk} = \frac{g'_k y''_{ij}}{\mu_D^2}$$

$$G'_{ijk} = \frac{g'_k y'_{ij} B_{D\bar{D}}^2}{\mu_D^4}$$

Interaction Lagrangian

$$G_{ijk}''' \lambda \bar{e}_i^* \bar{u}_j^* \bar{d}_k \quad (2)$$

$$G_{ijk}'' \mathcal{O} \bar{e}_i^* \bar{u}_j^* \bar{d}_k \quad (3)$$

gives corrections to the Majorana mass! \longrightarrow keep small

- CP violation is maximized when final states are indistinguishable

Focus on two terms:

$$G_{ijk} \lambda \ell_i q_j \bar{d}_k \quad (1)$$

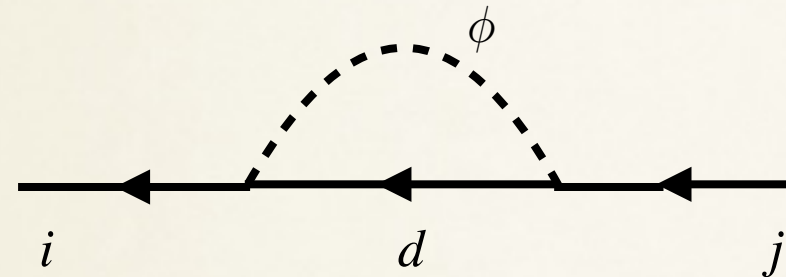
$$G'_{ijk} \mathcal{O} \ell_i q_j \bar{d}_k \quad (4)$$

$$\mathcal{L}_{\text{eff}} = \tilde{G}_\lambda \lambda \bar{d} q_1 \ell_2 + \tilde{G}_\mathcal{O} \mathcal{O} \bar{d} q_1 \ell_2$$

$$G_{211} \equiv \tilde{G}_\lambda, \quad G'_{211} \equiv \tilde{G}_\mathcal{O}$$

Pseudo-Dirac gluino self-energy

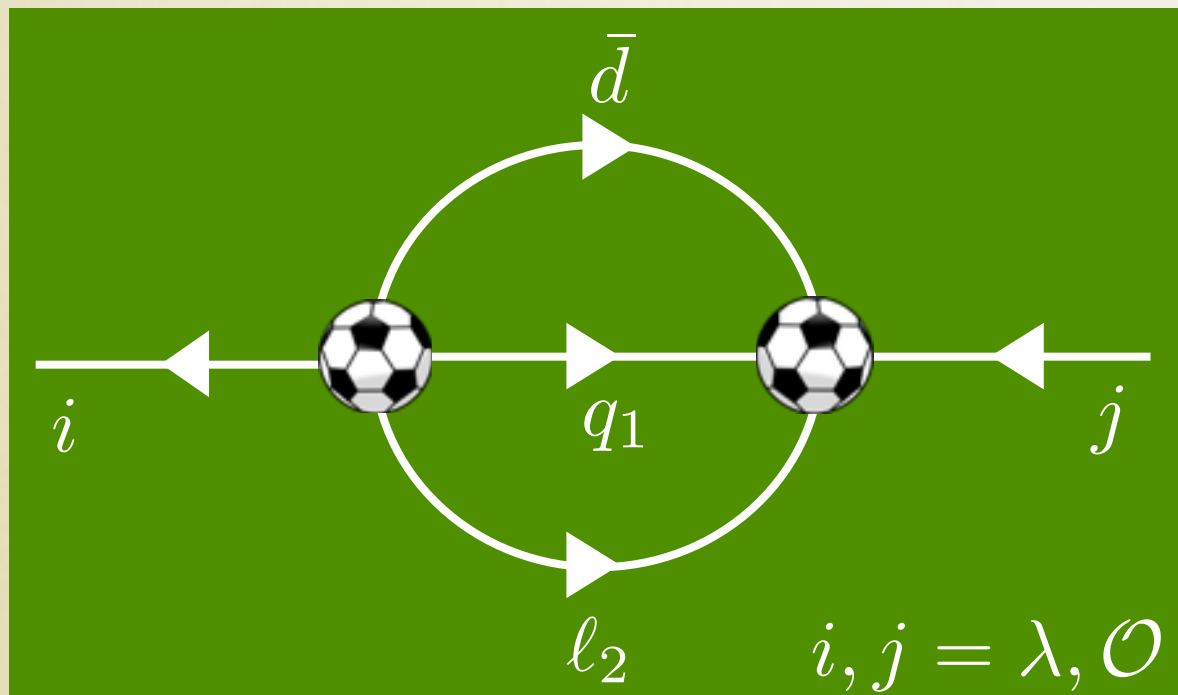
Toy model:



$$\Rightarrow H = M + \frac{i}{2}\Gamma$$

- Squarks are heavier than the gluino \rightarrow 1-loop self-energy is real
- Absorptive part at 2-loop order

$$\mathcal{L}_{\text{eff}} = \tilde{G}_\lambda \lambda \bar{d} q_1 \ell_2 + \tilde{G}_\mathcal{O} \mathcal{O} \bar{d} q_1 \ell_2$$



$$\Im \left(\frac{\Xi_{ij}}{\tilde{G}_i \tilde{G}_j^*} \right) = \frac{2p^4}{3(16\pi)^3}$$

soccer field diagram, David McKeen

Interaction Hamiltonian

Tree level masses + the soccer diagram = interaction Hamiltonian

$$H = M + \frac{i}{2}\Gamma$$

$$M = \begin{pmatrix} M_D & M_M \\ M_M^* & M_D \end{pmatrix}$$

corrections to the Majorana mass:

$$\delta_M \sim \frac{g_s g'_k}{(4\pi)^2} \left(\frac{\tilde{m}_k^2 B_{D\bar{D}}^2 + \mu_D^2 B_{D\bar{d}_k}^2}{\mu_D^4} \right) M_D$$

$$\Gamma \simeq \begin{pmatrix} \Gamma_0 & 0 \\ 0 & \Gamma_0 \end{pmatrix} + \frac{M_D^5}{12 (8\pi)^3} \begin{pmatrix} |\tilde{G}_\lambda|^2 + |\tilde{G}_\mathcal{O}|^2 & 2\tilde{G}_\lambda^* \tilde{G}_\mathcal{O} \\ 2\tilde{G}_\lambda \tilde{G}_\mathcal{O}^* & |\tilde{G}_\lambda|^2 + |\tilde{G}_\mathcal{O}|^2 \end{pmatrix}$$

Γ_0 = non \mathcal{L}_{eff} decays
e.g. gluon and gravitino

absorptive part of the soccer diagram

Oscillations

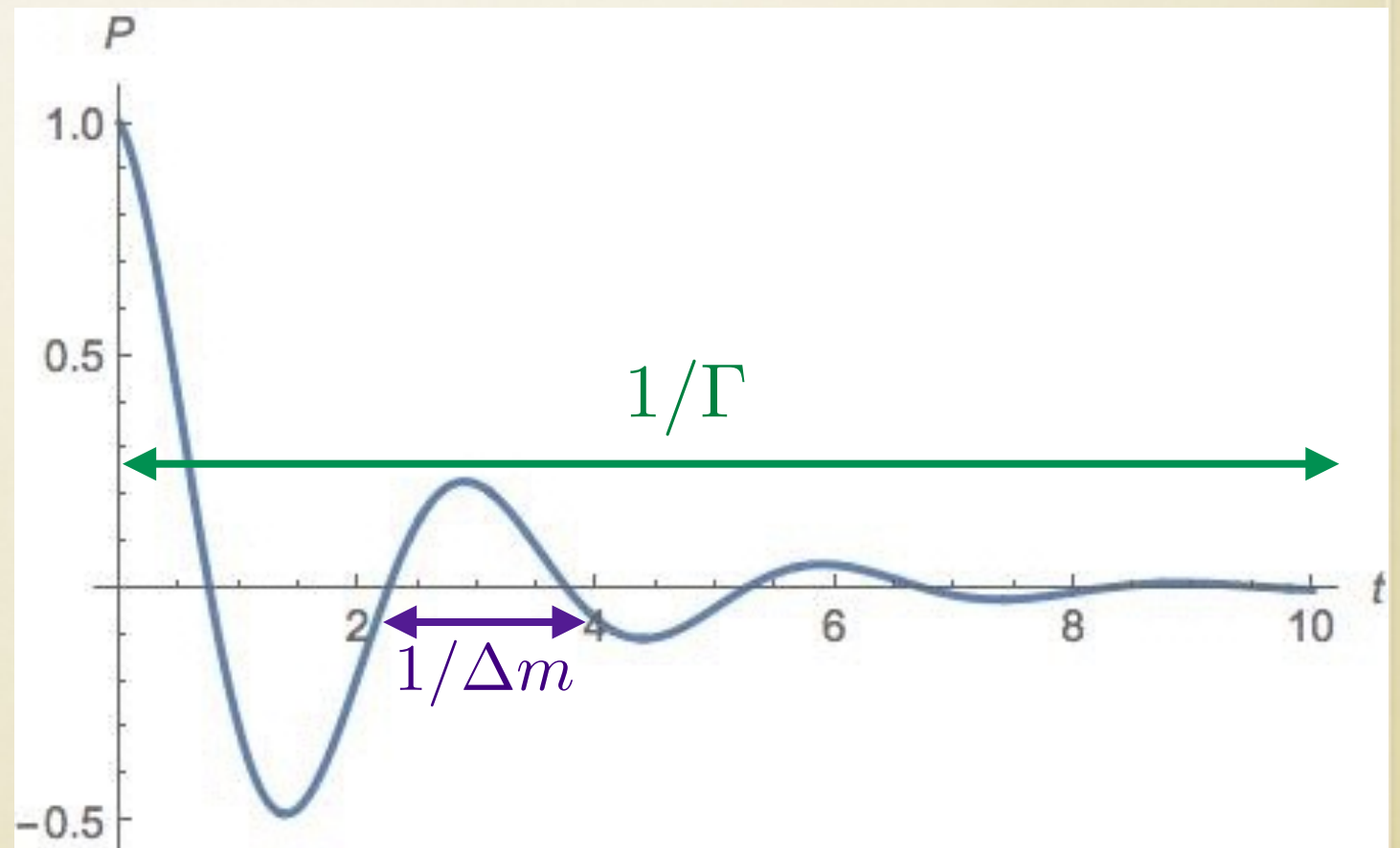
$H = M + \frac{i}{2}\Gamma \rightarrow$ similar to neutral meson mixing Hamiltonian

- Eigenvectors: $|\psi_H\rangle = p|\psi\rangle - q|\bar{\psi}\rangle$
 $|\psi_L\rangle = p|\psi\rangle + q|\bar{\psi}\rangle$, with eigenvalues: $\omega_{H,L}$
 $H = \text{heavy}, L = \text{light}$
- Important: mass difference and the width

$$\Delta m = m_H - m_L = \Re(\omega_H - \omega_L)$$

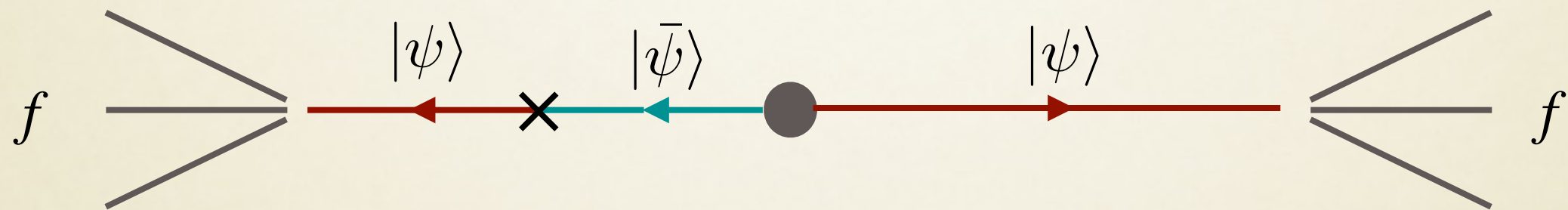
$$x \equiv \frac{\Delta m}{\Gamma}$$

- $x \ll 1$: decay before oscillation
- $x \gg 1$: rapid oscillations
- $x \sim 1$: observe nice oscillations before decay

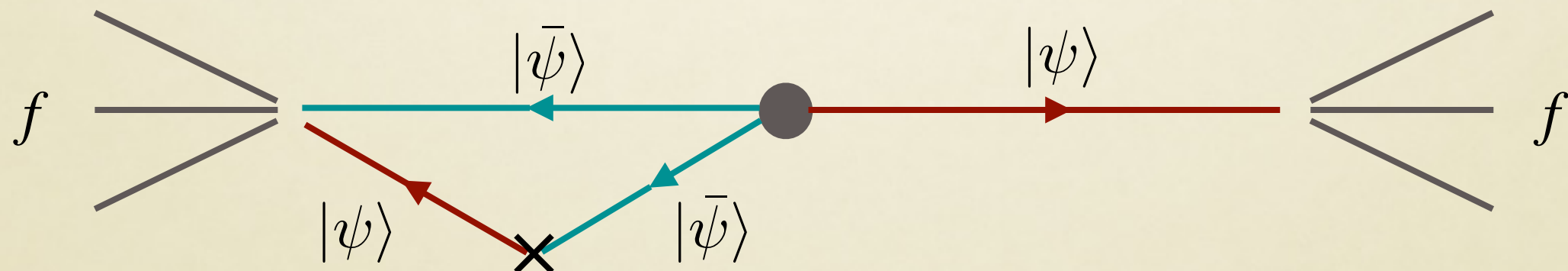


CP Violation in Oscillations

- *CP* violation needs a relative phase between M and Γ
- Two ways to get *CP* violation:
 1. In mixing: $|q/p| \neq 1$



2. In interference between decays with mixing and without mixing:

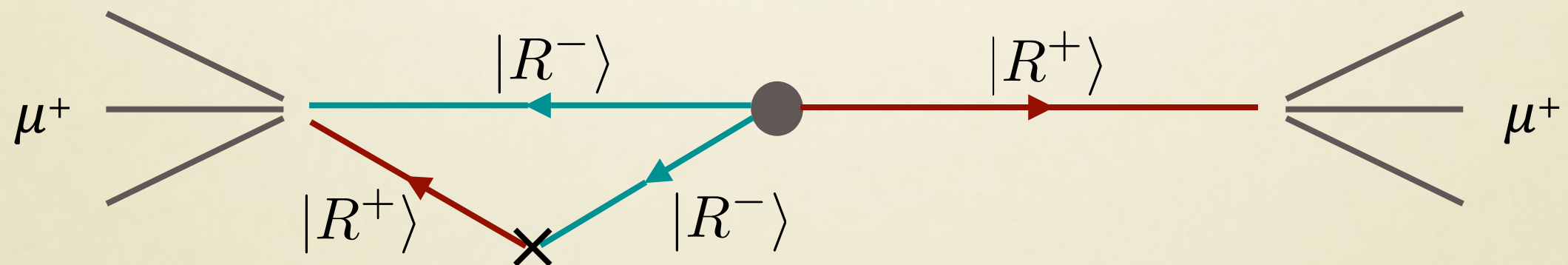


CP violation in gluino oscillations

$$\mathcal{L}_{\text{eff}} = \tilde{G}_\lambda \lambda \bar{d} q_1 \ell_2 + \tilde{G}_\mathcal{O} \mathcal{O} \bar{d} q_1 \ell_2 + \text{h.c.}$$

both states can decay into the same final state

can have CP violation in interference between decays
with mixing and without mixing



$|R^\pm\rangle$ = state with ± 1 $U(1)_R$ charge

Same-sign dimuon asymmetry

- CP violation can be observed as a same-sign dimuon asymmetry:

$$A \equiv \frac{N^{++} - N^{--}}{N^{++} + N^{--}}$$

N^{++} = number of events with two positively charged muons

$A < 1$: more muons than antimuons \longrightarrow CP violation!

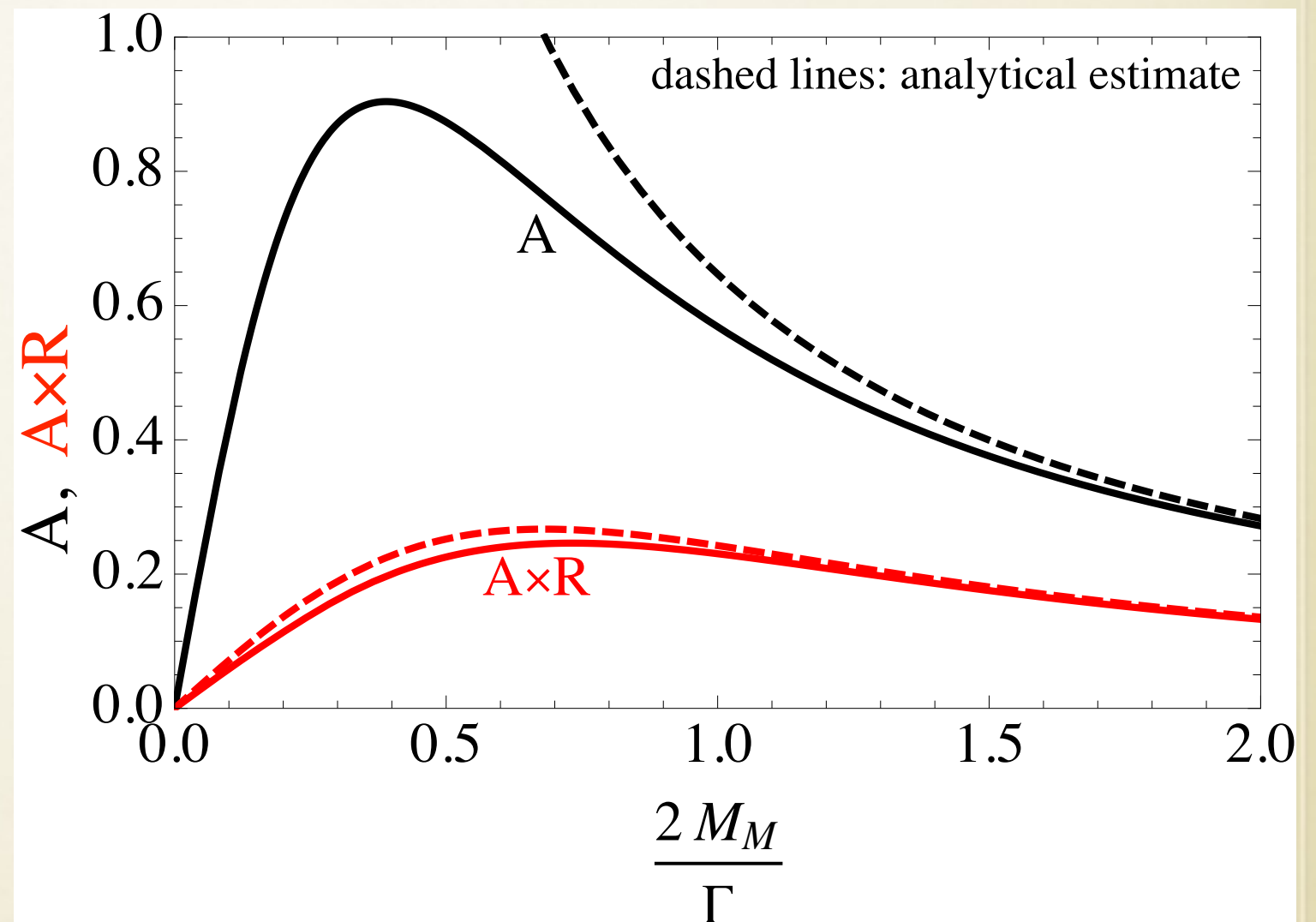
- Also important: fraction of same sign muon decays:

$$R \equiv \frac{N^{++} + N^{--}}{N^{+-} + N^{-+} + N^{++} + N^{--}}$$

$A \times R \propto$ how much asymmetry one can expect

Let's talk numbers

- ▶ gluino mass = 1.6 TeV
- ▶ scalar mass (μ_D) = 5 TeV
- ▶ squark mass ($m_{\phi d}$) = 4 TeV
- ▶ gluino width (Γ) = 300 eV
- ▶ gravitino mass = 5 keV
- ▶ gravitino decays (Γ_0) small
- ▶ $\phi_\Gamma \equiv \arg \Gamma_{12} = -\pi/3$
- ▶ $\Delta m \simeq 2M_M$



100 fb⁻¹, @13 TeV: gluino production cross-section = 16 fb
400 same sign dimuon events for $R = 0.25$
Can probe $O(10-20\%)$ asymmetry

Summary

- Pseudo-Dirac fermions are a feature of $U(1)_R$ symmetric SUSY
- They have particle—antiparticle oscillations
- There can be CP violation in the decays of oscillating pseudo-Dirac fermions
- This CP violation can be observed as a same-sign dimuon asymmetry at the LHC
- New sources of CP violation are always welcome! (baryogenesis)
- Similar CP violating effects can be present in other systems, e.g. mesino oscillations